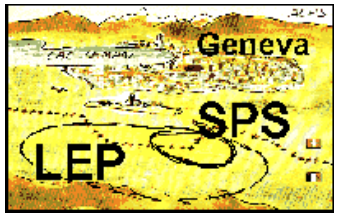
Results on Photon Structure Functions from

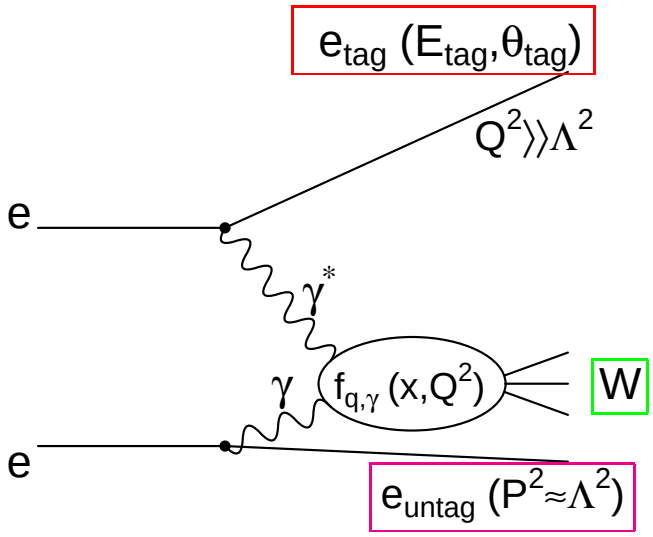


Richard Nisius, CERN

Jerusalem, 20 August 1997

- Lepton pairs and $F^{\gamma}_{\mathrm{k,QED}}$, k = 2,A,B
- Hadronic $F^{\gamma}_{2}(x, Q^2)$

Electron-Photon Scattering



$$\frac{d^2\sigma_{e\gamma\to eX}}{dx\,dQ^2} = \frac{2\pi\alpha^2}{x\,Q^4}\cdot$$

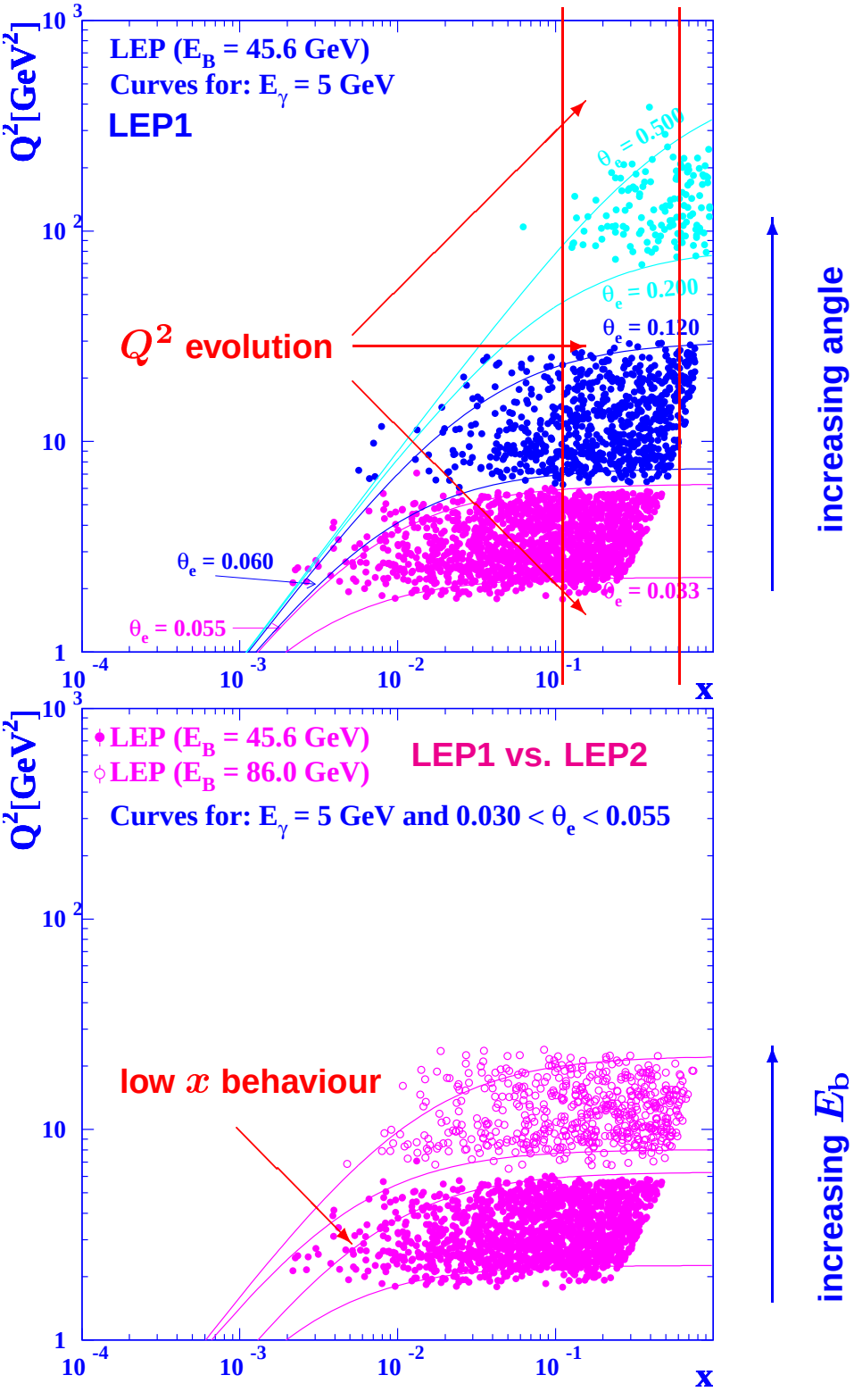
$$\left[(1+(1-y)^2)\,F_2^\gamma(x,Q^2) - \underbrace{y^2 F_L^\gamma(x,Q^2)}_{\to 0}\right]$$

$$Q^2 = 2\,E_b\,E_{tag}\,(1-\cos\theta_{tag}) \gg P^2$$

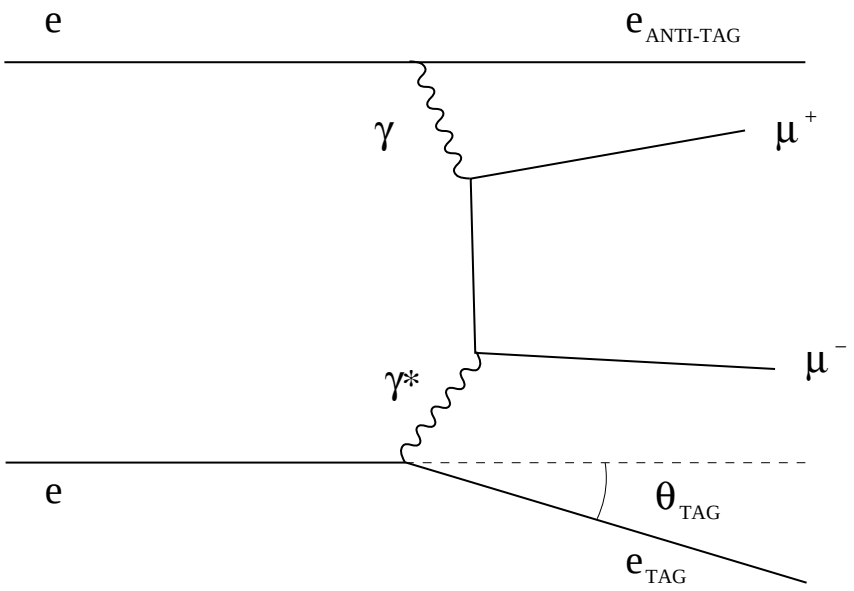
$$x = \frac{Q^2}{Q^2+W^2+P^2}$$

$$y = 1 - \frac{E_{tag}}{E_b}\cos^2\left(\frac{\theta_{tag}}{2}\right) \ll 1$$

The $x - Q^2$ plane



The production of lepton pairs



$$\frac{d^2\sigma_{e\gamma\to e\mu^+\mu^-}}{dx\,dQ^2} =$$

$$\frac{2\pi\alpha^2}{x\,Q^4}\left[\left(1+(1-y)^2\right)F^{\gamma}_{2,\mathrm{QED}} - y^2 F^{\gamma}_{\mathrm{L,QED}}\right]$$

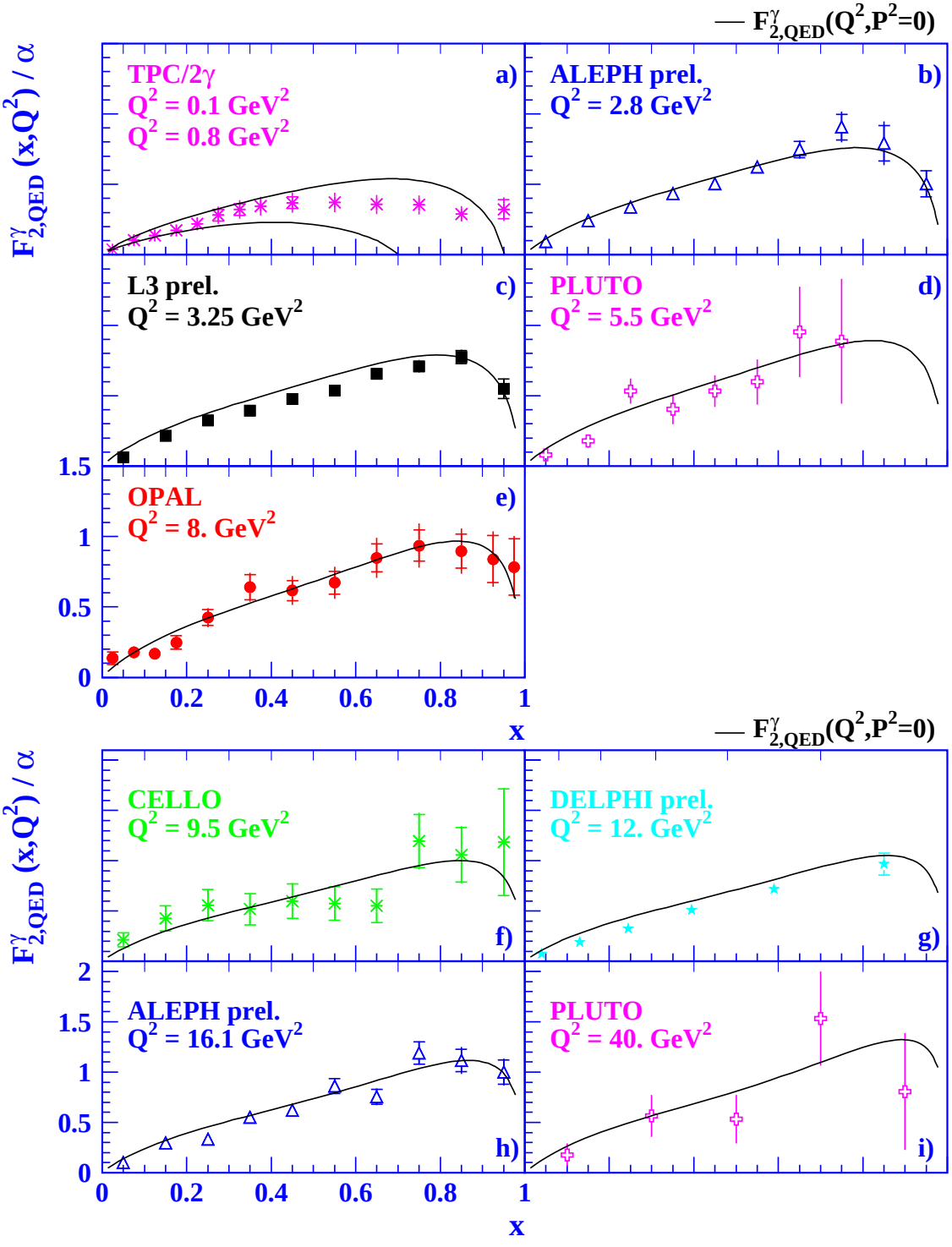
$$F^{\gamma}_{2,\mathrm{QED}}(x,Q^2,P^2)/\alpha \approx$$

$$\frac{x}{\pi}\left[1 - 2x(1-x)\ln\frac{W^2}{m_\mu^2+x(1-x)P^2} - 1 + 8x(1-x) - \frac{x(1-x)P^2}{m_\mu^2+x(1-x)P^2}\right]$$

$$F^{\gamma}_{\mathrm{L,QED}}(x,Q^2,P^2=0)/\alpha \approx \frac{4}{\pi}x^2(1-x)$$

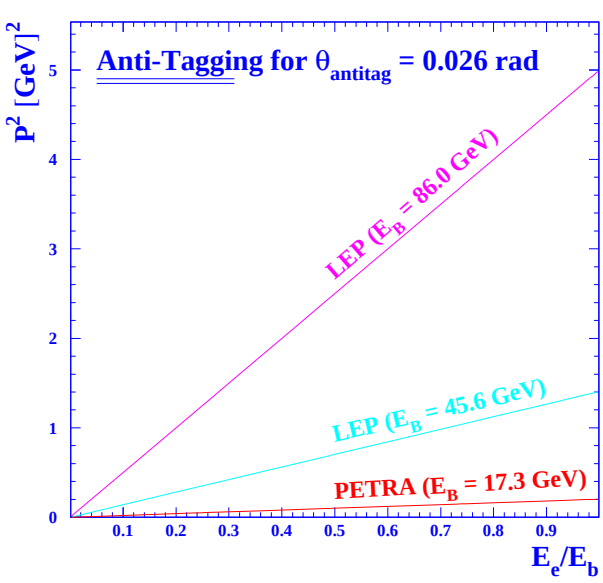
$\Rightarrow$ **QED is a well suited study ground for structure function analysis**

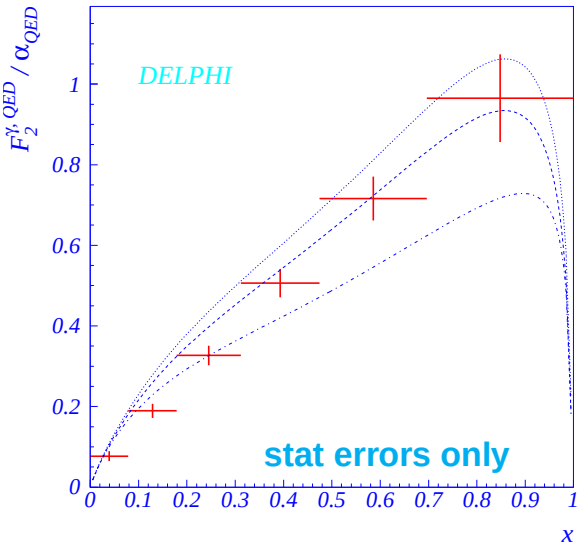
Measurements of $F_{2,\mathrm{QED}}^{\gamma}$

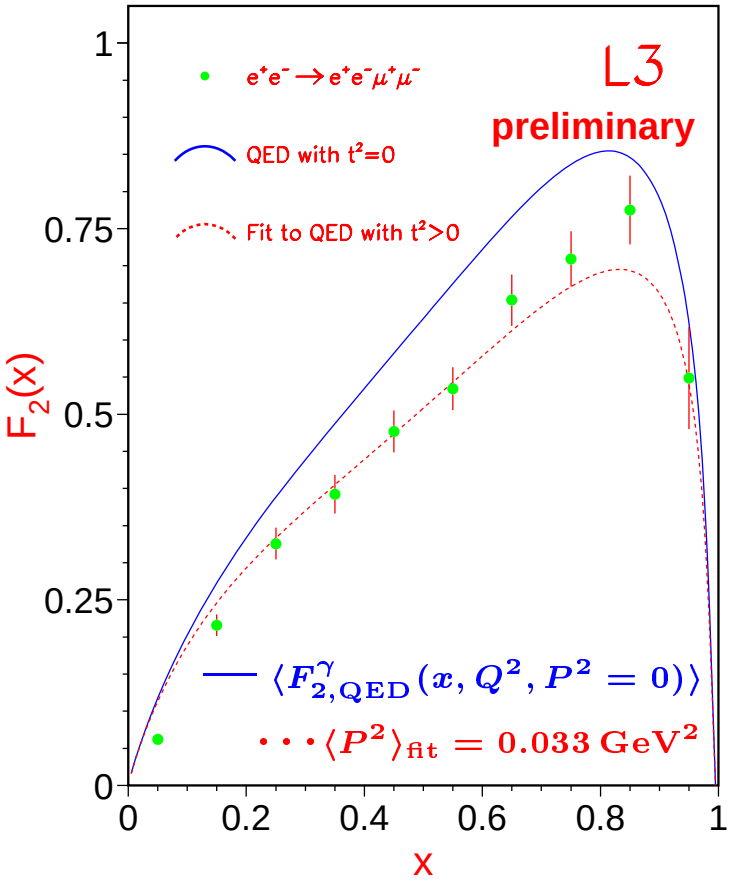


All results are according to expectations from QED

$F_{2,\mathrm{QED}}^{\gamma}$ for virtual photons

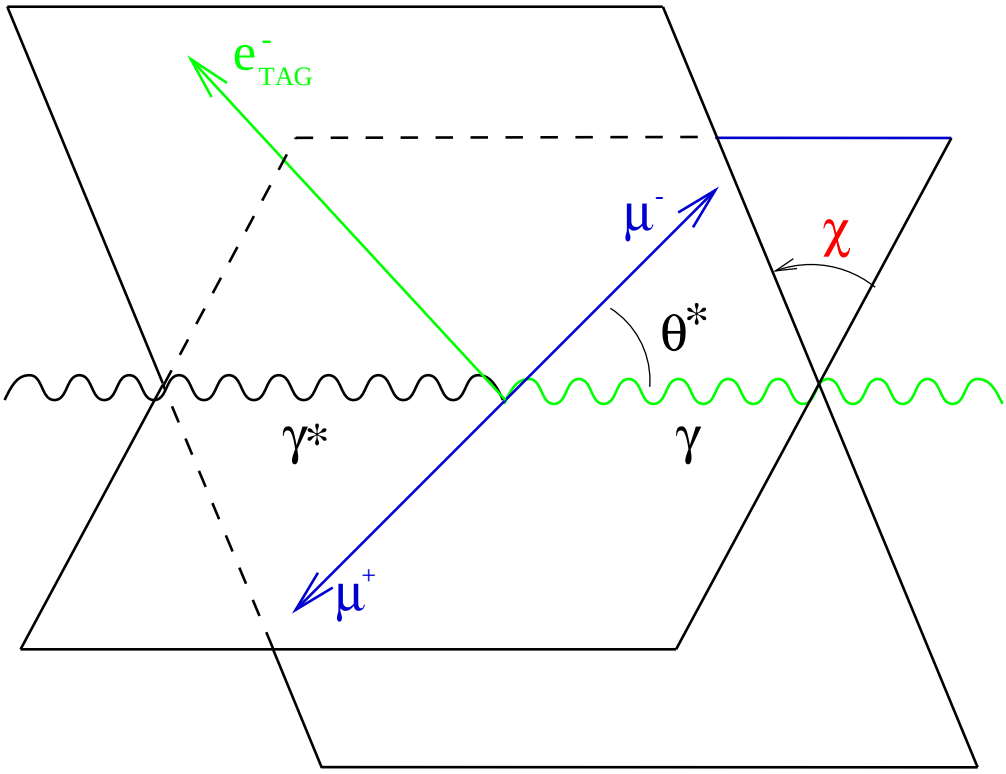






For $F_{2,\mathrm{QED}}^{\gamma}$ the effect of the photon virtuality P^2 is clearly seen

Azimuthal Correlations



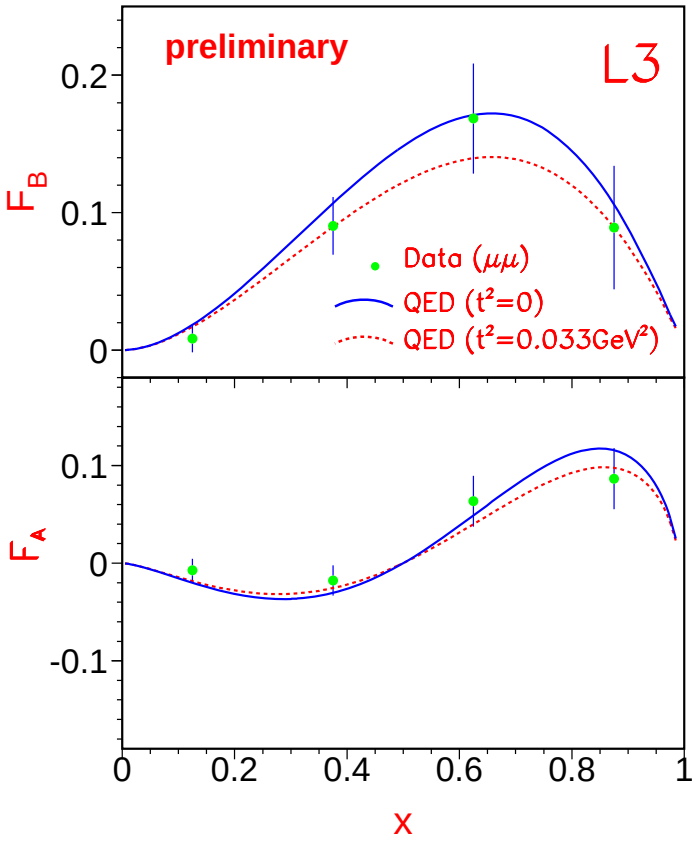
$$e\gamma \to e\mu^+\mu^-$$

$$d\sigma \propto \left(1 + (F_A^\gamma/F_2^\gamma)\cdot\cos\chi + \frac{1}{2}\epsilon(F_B^\gamma/F_2^\gamma)\cdot\cos 2\chi\right)$$

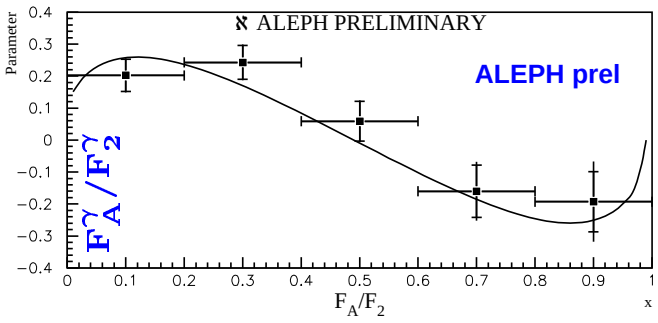
$$\tfrac{1}{2}\epsilon = \tfrac{(1-y)}{1+(1-y)^2} \approx 1$$

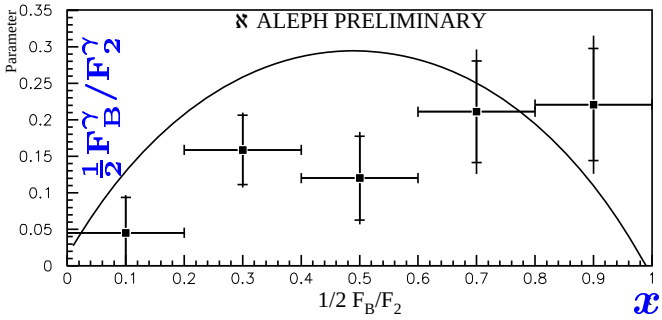
The χ dependence gives access to other structure functions besides $F_{2,\mathrm{QED}}^\gamma$

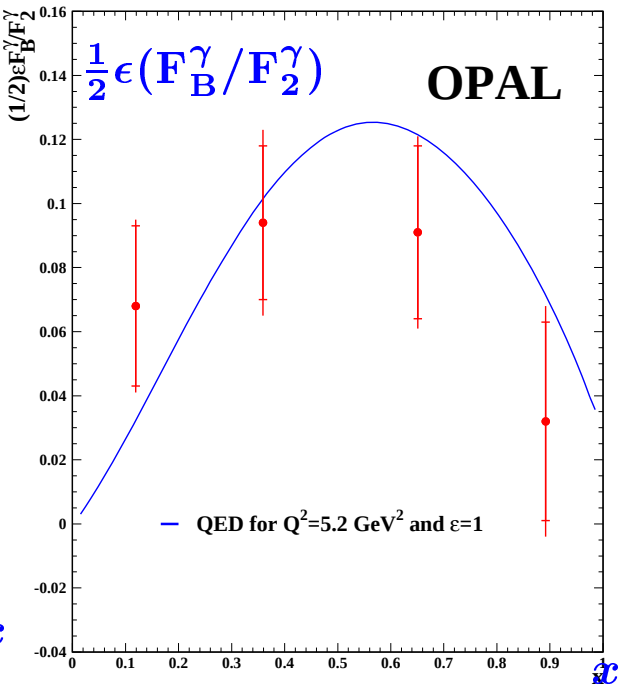
Other QED structure functions



Results for 1994 Data

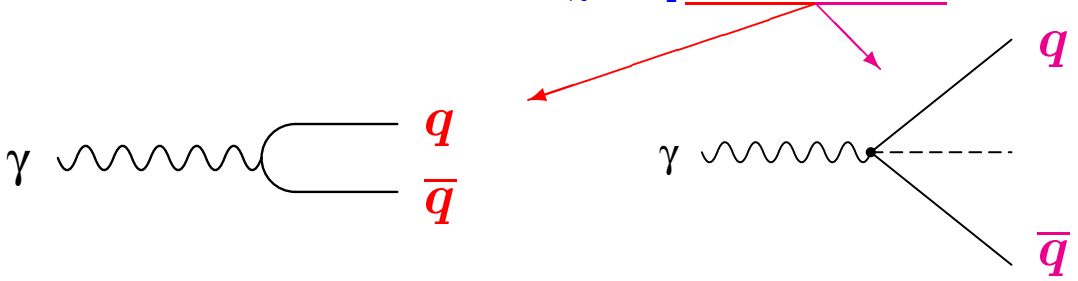






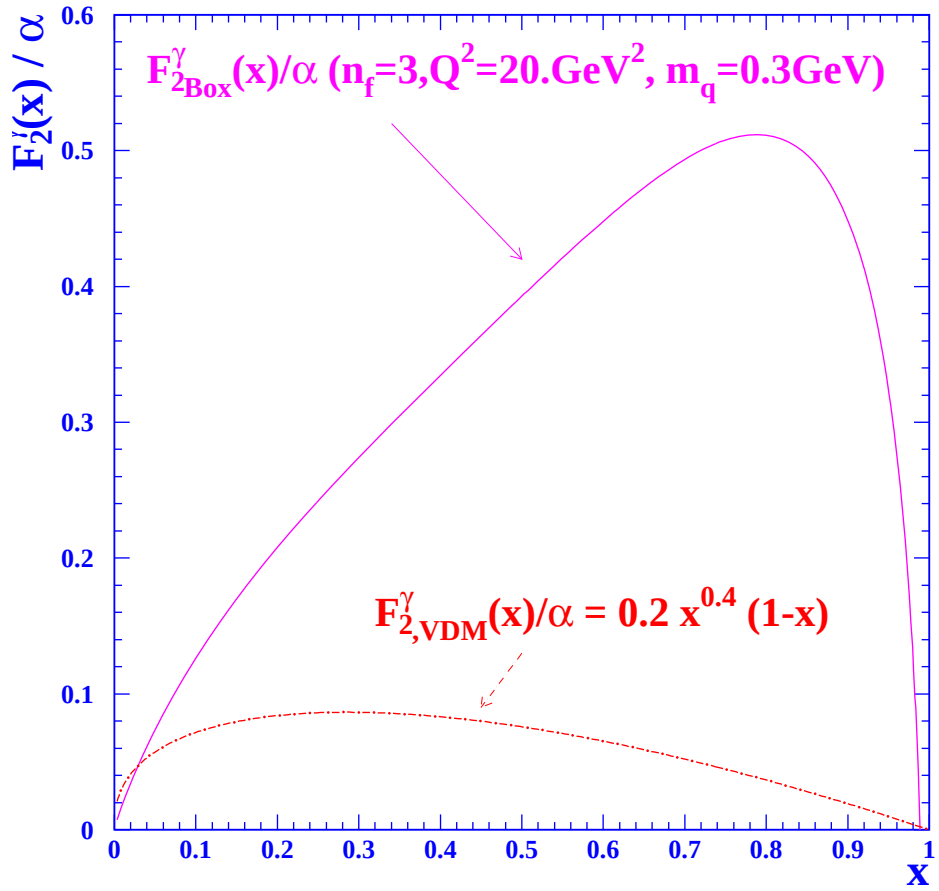
The contributions to $F_2^\gamma(x, Q^2)$

$$F_2^\gamma(x, Q^2) = x \sum_{c,f} e_q^2 \, f_{q,\gamma}(x, Q^2)$$



'hadronic', p_T = "small"
non–perturbative
VDM (ρ, ω, ϕ)

'pointlike', p_T = "large"
perturbative



The general procedure to measure F_2^γ

1. Events are triggered with high efficiency by the luminosity detectors nearly independent of the hadronic final state.

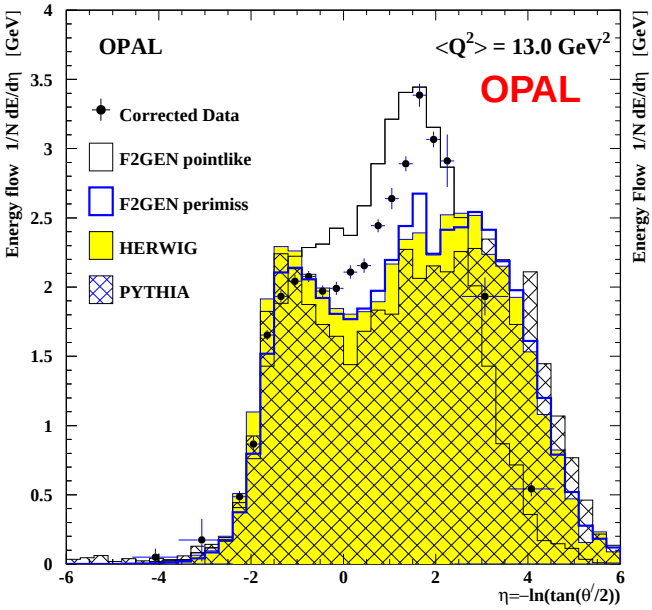
2. Q^2 is accurately measured from the electron.

3. E_γ is unknown and varies from event to event
   $\Rightarrow W_{\mathrm{vis}}$ has to be measured from the hadrons.
   (No electron alone method as e.g. at HERA)

4. x is obtained from x_{vis} via unfolding (Blobel, ...)
   $\Rightarrow$ Dependence on the formation of the hadronic final state as assumed by the Monte Carlo models!
   (For details see talk by J. A. Lauber Pa2)

The model dependence

$1/N\,\mathrm{d}E/\mathrm{d}\eta$



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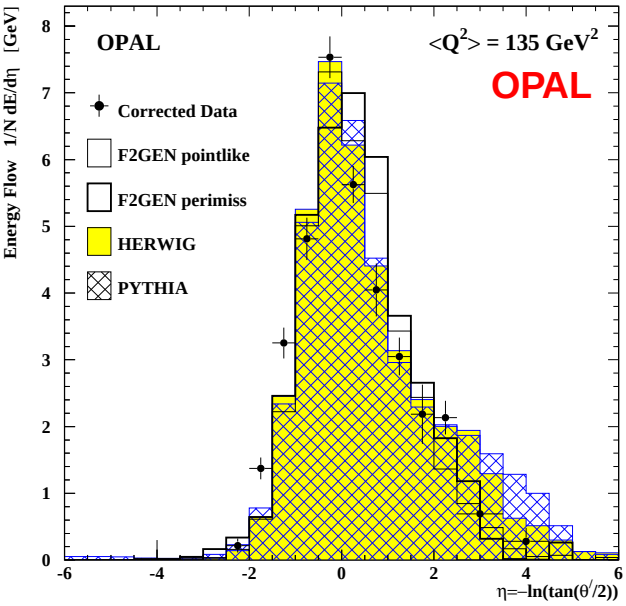
$1/N\,\mathrm{d}E/\mathrm{d}\eta$



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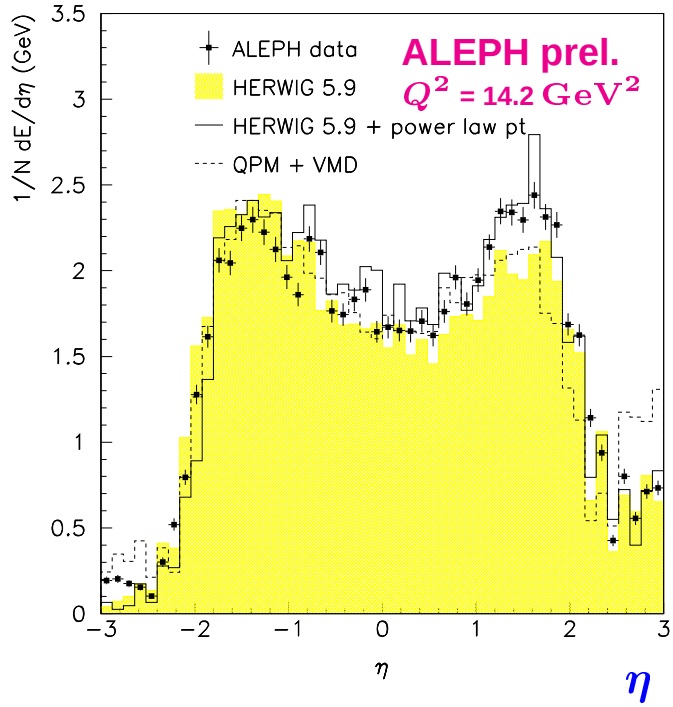

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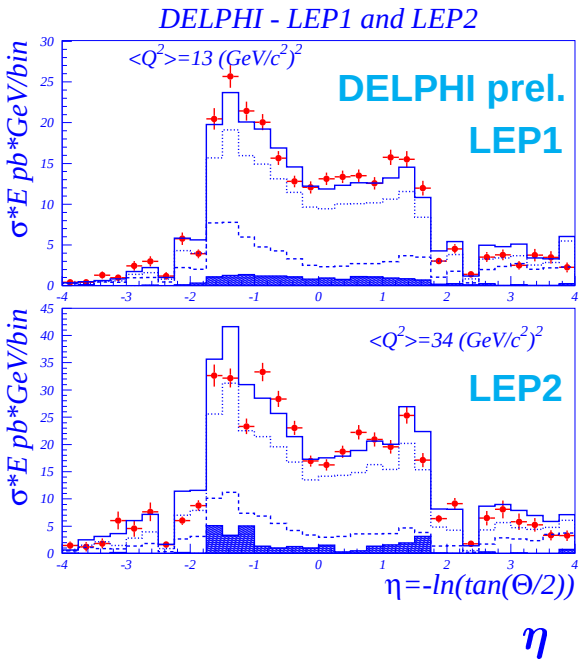

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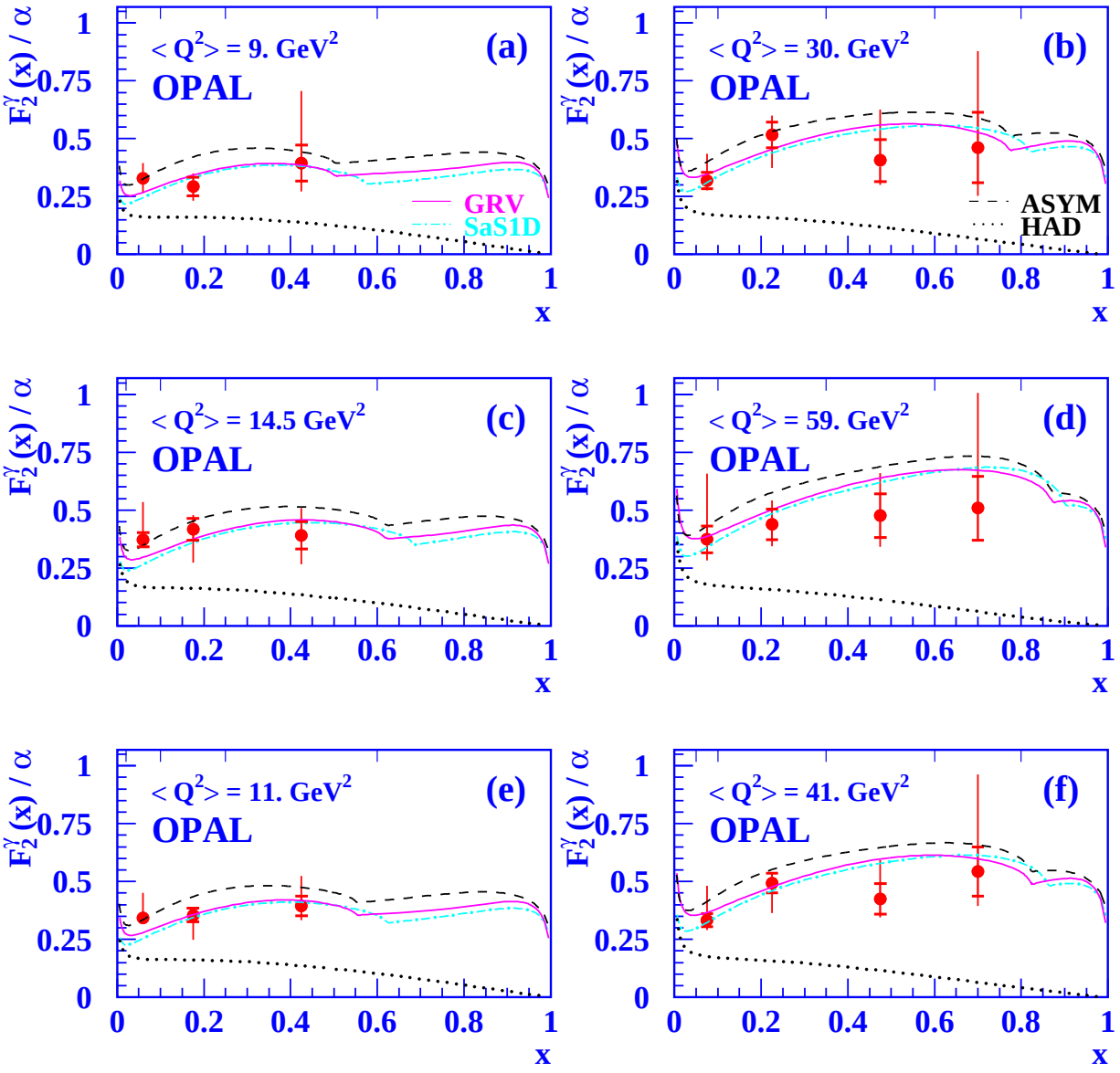
Improvements on the Monte Carlo programs are needed

F_2^γ compared to various models



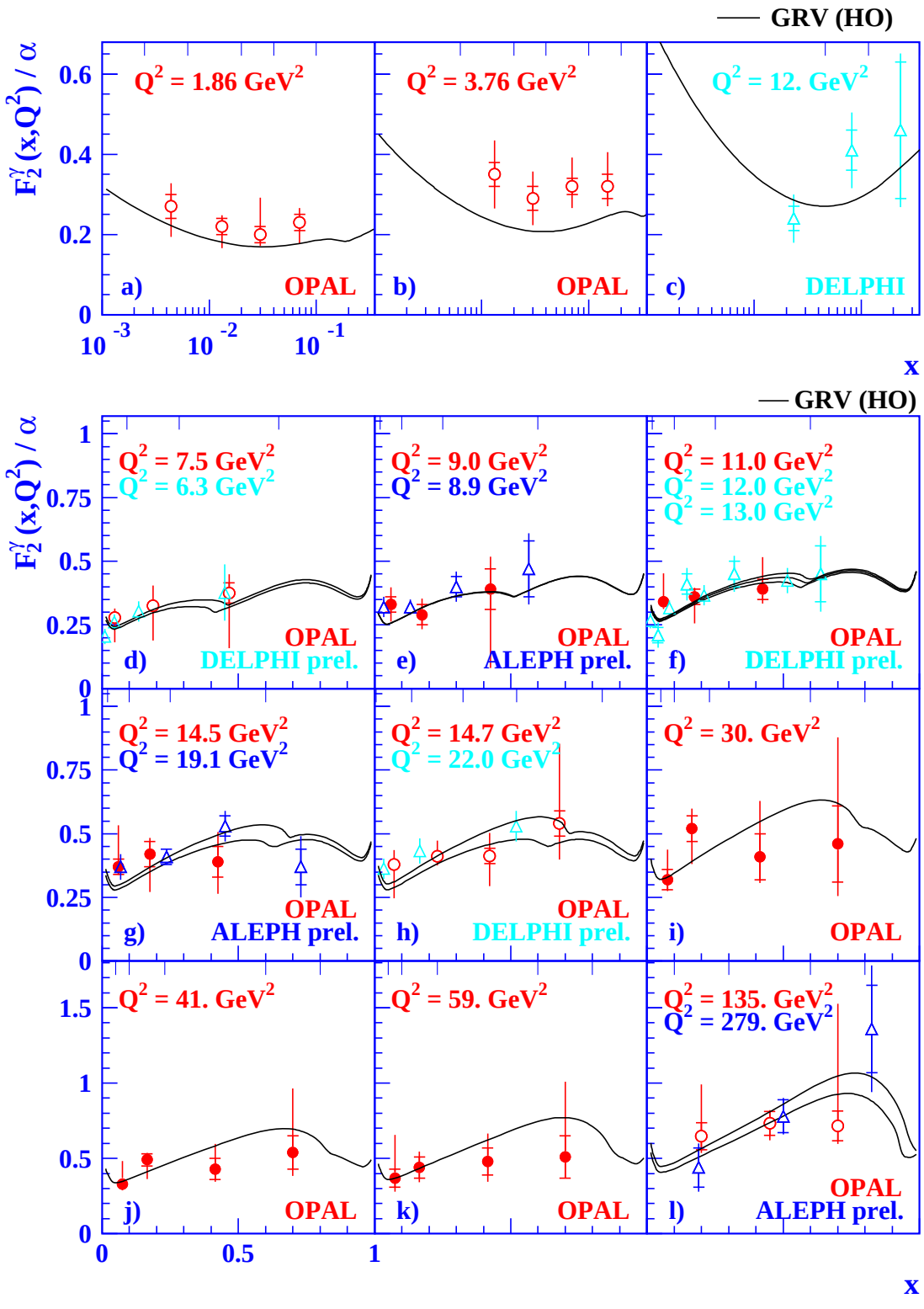
ASYM $\equiv$ asymptotic solution for n_f = 3 (Witten LO)

$\oplus$ massive charm (Bethe Heitler LO) $\oplus$ HAD (GRV VDM LO)

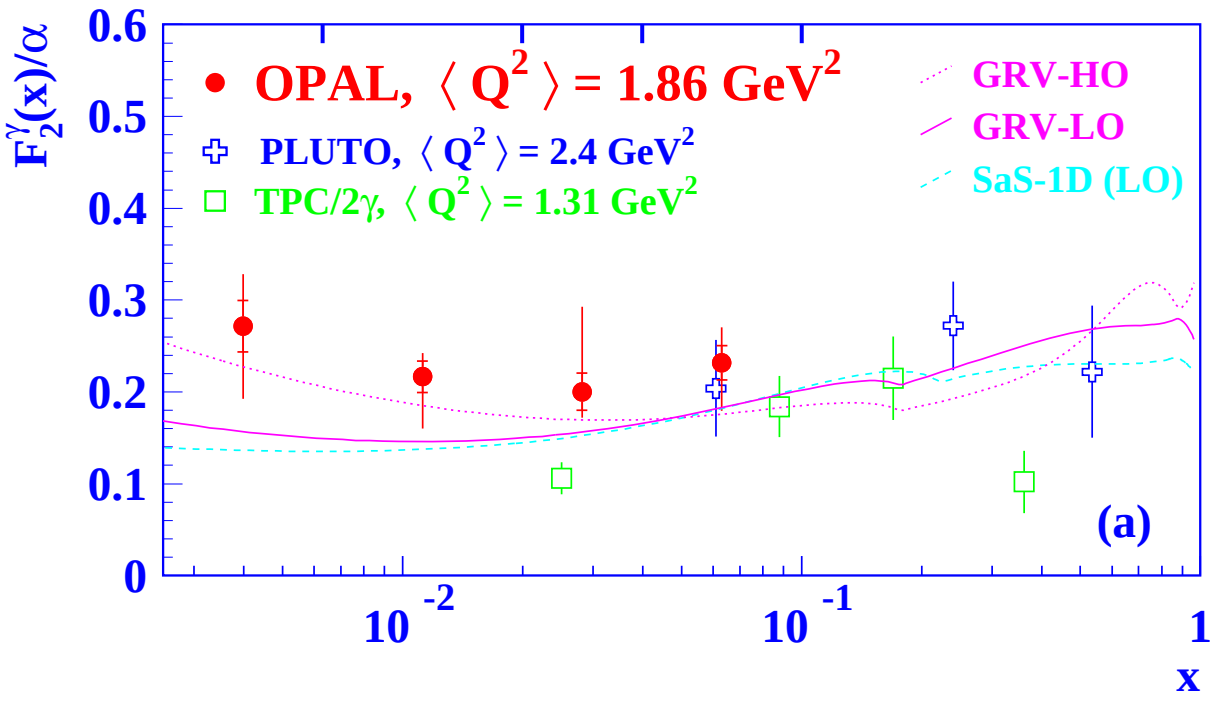
GRV $\equiv$ Glück, Reya, Vogt LO

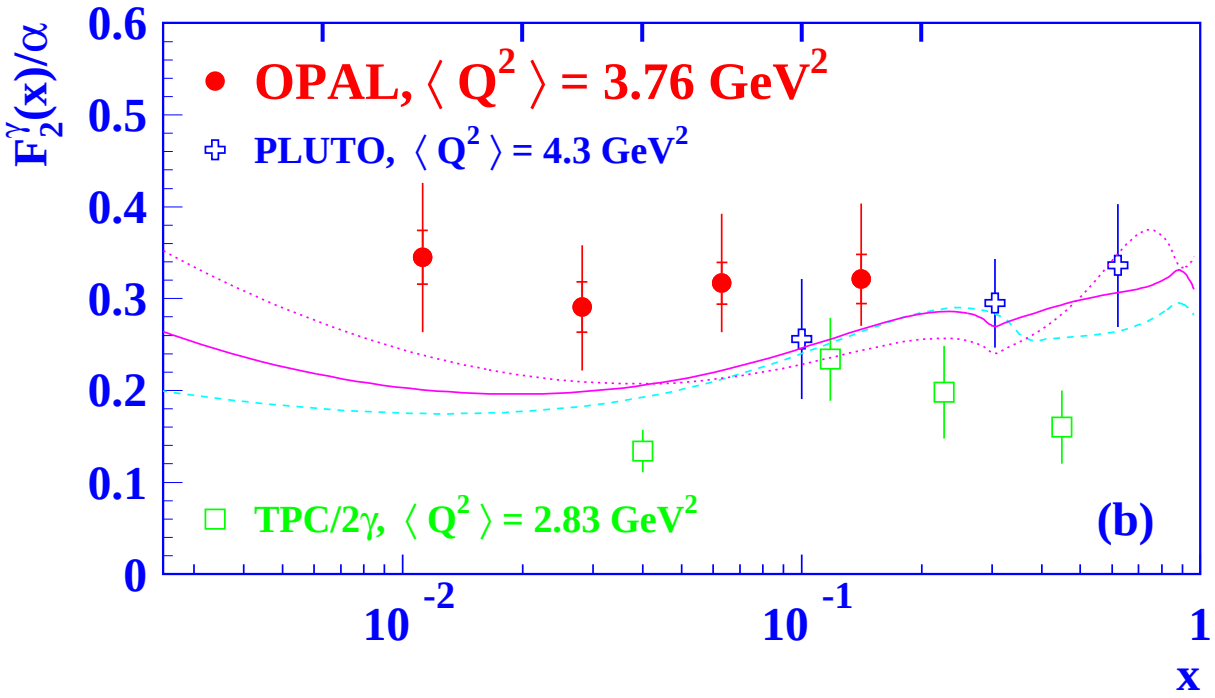
SaS $\equiv$ Schuler, Sjöstrand SaS1D LO

The LEP data on F_2^γ



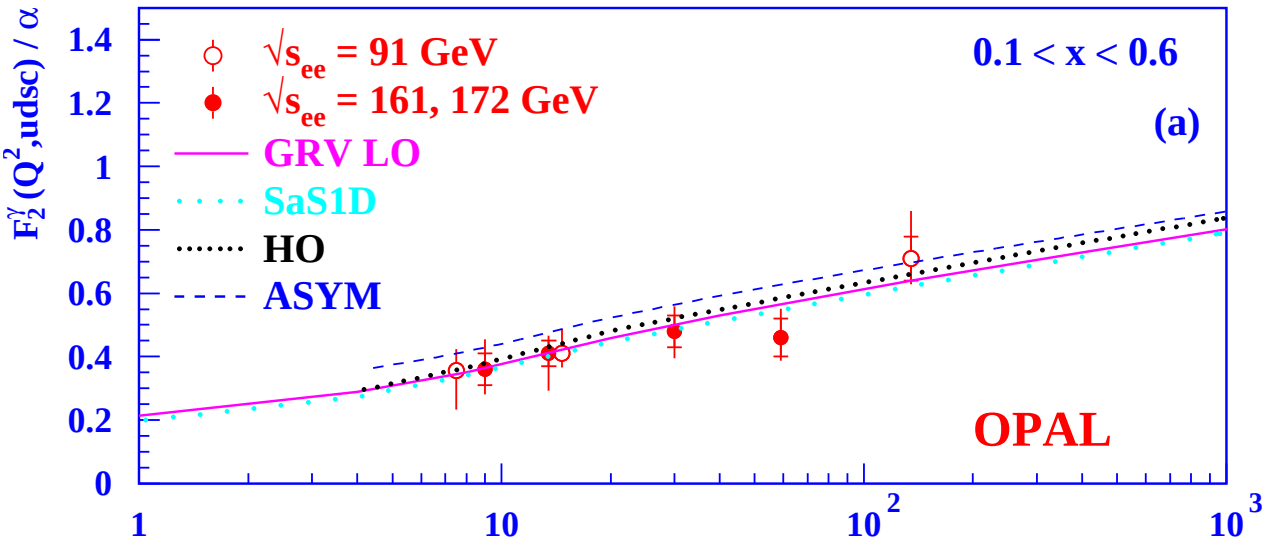
The region of low x and Q^2

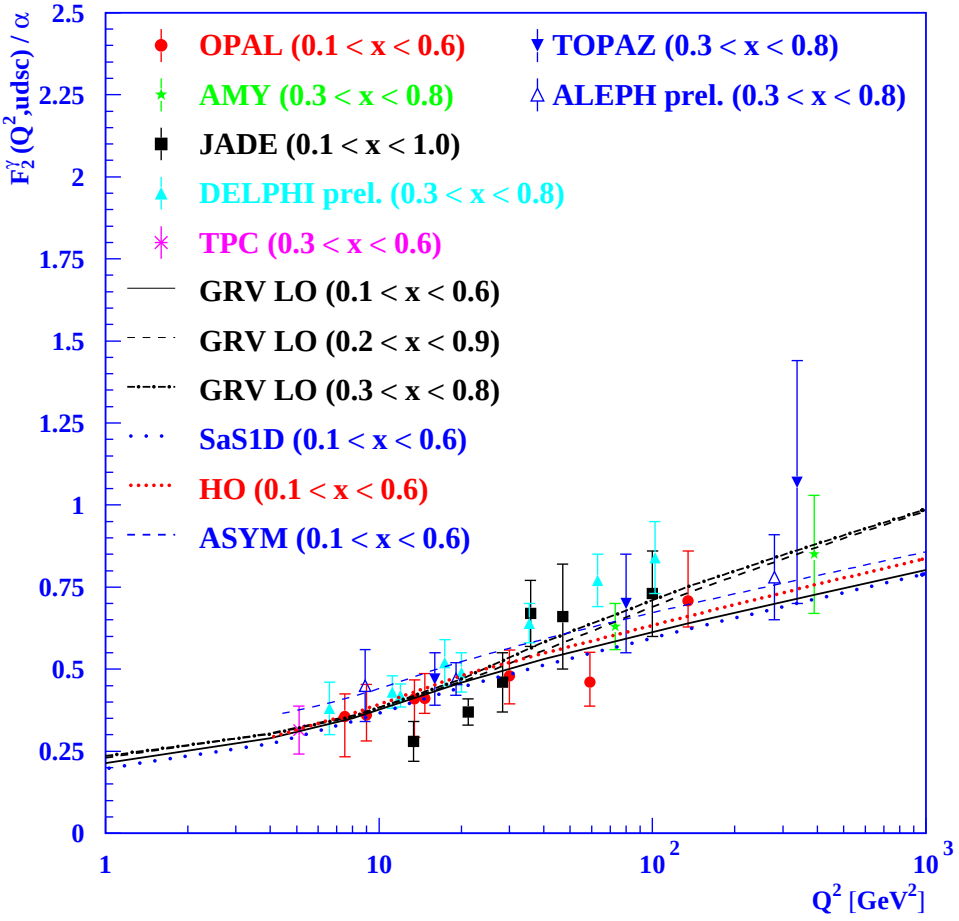




The Q^2 evolution of F_2^γ

$$F_2^\gamma = (0.16 \pm 0.05^{+0.17}_{-0.16}) + (0.10 \pm 0.02^{+0.05}_{-0.02}) \ln(Q^2/\mathrm{GeV}^2)$$





Conclusions

1. QED structure functions are in nice agreement with the data.
2. The determination of the hadronic structure function is very difficult. Monte Carlo models need to be improved to bring the systematic errors down for the regions of low- and high-x.
3. The evolution of F_2^γ with Q^2 is found to be logarithmic, as predicted by QCD, but precision tests of $\mathrm{d}(F_2^\gamma/\alpha)/\mathrm{d}\ln Q^2$ are not yet in sight.
4. Structure function measurements are a very active field at LEP with good prospects for the LEP2 programme.

I would like to thank the LEP Collaborations, especially C. Brew, A. Finch, S. Söldner Rembold, G. Susinno and A. Wright.

slides:

http://wwwcn1.cern.ch/~nisius/talks/JERU200897/index.html